

# VIRTUAL EAST-WEST SCV SEMINAR

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## INFINITESIMAL CR AUTOMORPHISMS OF STRICTLY POSITIVE WEIGHT FOR POLYNOMIAL MODELS AND THEIR CONSEQUENCES

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Let  $M_H$  be the hypersurface given by

$$M_H = \{(z, w) \in \mathbb{C}^{n+1} \mid \Im w = \langle z, z \rangle\},$$

where  $\langle z, z \rangle$  is a nondegenerate Hermitian form. We recall the following classical statement contained in the work of Chern and Moser in 1974:

**Theorem.** Let  $M \subset \mathbb{C}^{n+1}$  be a real hypersurface that is a real-analytic perturbation of  $M_H$ , and let  $F$  and  $G$  be two germs of biholomorphic maps preserving  $M$ . Then, if  $F$  and  $G$  have the same 2-jets at  $p$ , they coincide.

In this talk, I will discuss the following questions:

- (1) What happens to this theorem if we replace the Hermitian form by a real (well chosen) homogeneous polynomial  $P$ , that is, if one considers perturbations of the model hypersurface given by

$$M_H = \{(z, w) \in \mathbb{C}^{n+1} \mid \Im w = P(z, \bar{z})\}?$$

- (2) What happens to this theorem if we replace the hypersurface  $M_H$  by the submanifold of codimension  $d$  given by

$$M_H = \{(z, w) \in \mathbb{C}^{n+d} \mid \Im w = \langle z, z \rangle\},$$

where  $\langle z, z \rangle$  is a  $d$ -dimensional nondegenerate Hermitian form?

This talk involves work with Martin Kolar and Dmitri Zaitsev for the first question, with Florian Bertrand, Lea Blanc-Centi and Jan Gregorovic for the second question.

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