

On MATLAB command: **dsolve**

The MATLAB command `dsolve` computes symbolic solutions to ordinary differential equations.

Syntax

```
dsolve('eq1','eq2',...,'cond1','cond2',...,'v')
```

Description

`dsolve('eq1','eq2',...,'cond1','cond2',...,'v')` symbolically solves the ordinary differential equations `eq1`, `eq2`,... using `v` as the independent variable. Here `cond1`, `cond2`,... specify boundary or initial conditions or both. You also can use the following syntax:

```
dsolve('eq1, eq2',...,'cond1,cond2',...,'v').
```

The default independent variable is `t`.

The letter `D` denotes differentiation with respect to the independent variable. The primary default is d/dx . The letter `D` followed by a digit denotes repeated differentiation. For example, `D2` is d^2/dx^2 . Any character immediately following a differentiation operator is a dependent variable. For example, `D3y` denotes the third derivative of $y(x)$ or $y(t)$.

You can specify initial and boundary conditions by equations like $y(a) = b$ or $Dy(a) = b$, where y is a dependent variable and a and b are constants. If the number of the specified initial conditions is less than the number of dependent variables, the resulting solutions contain the arbitrary constants `C1`, `C2`,...

You can input each equation or a condition as a separate symbolic equation.

The `dsolve` command accepts up to 12 input arguments.

`dsolve` can produce the following three types of outputs:

- For one equation and one output, `dsolve` returns the resulting solution with multiple solutions to a nonlinear equation in a symbolic vector.

- For several equations and an equal number of outputs, `dsolve` sorts the results alphabetically and assigns them to the outputs.

- For several equations and a single output, `dsolve` returns a structure containing the solutions.

If `dsolve` cannot find a closed-form (explicit) solution, it attempts to find an implicit solution. When `dsolve` returns an implicit solution, it issues a warning. If `dsolve` cannot find either an explicit or an implicit solution, then it issues a warning and returns the empty `sym`. In such a case,

you can find a numeric solution, using the MATLAB [ode45](#) functions (we will learn how to use it later). In some cases involving nonlinear equations, the output is an equivalent lower order differential equation or an integral.

Example 1: Solve

$$\frac{dy}{dt} = 2*y + t$$

Solution:

```
>> dsolve('Dy=2*y+t','t')
```

ans =

```
(C7*exp(2*t))/4 - t/2 - 1/4
```

Or

```
>> dsolve('Dy=2*y+t')
```

ans =

```
(C7*exp(2*t))/4 - t/2 - 1/4
```

Remark: the default independent variable is t, if you do not specify in the command.

Example 2: Solve

$$\frac{dy}{dt} = 2*y + t, y(0) = 1$$

Solution:

```
>> dsolve('Dy=2*y+t','y(0)=1','t')
```

ans =

```
(5*exp(2*t))/4 - t/2 - 1/4
```

Example 3: Solve

$$\frac{dy}{dx} = 2 * y + x^2, y(0) = 1$$

```
>> dsolve('Dy=2*y+x^2','y(0)=1','x')
```

ans =

$$(5 * \exp(2 * x)) / 4 - x / 2 - x^2 / 2 - 1 / 4$$

Example 4: Solve

$$\frac{d^2 y}{dx^2} + 2 \frac{dy}{dx} = e^x, y(0) = 1, y'(0) = 0$$

Solution:

```
>> dsolve('D2y+2*Dy=exp(x)','y(0)=1','Dy(0)=0','x')
```

ans =

$$1 / (6 * \exp(2 * x)) + \exp(x) / 3 + 1 / 2$$

Example 5: Solve

$$\frac{d^2 y}{dx^2} + 2 \frac{dy}{dx} = \sin(x), y(0) = -1, y'(0) = 1$$

Solution:

```
>> dsolve('D2y+2*Dy=sin(x)','y(0)=-1','Dy(0)=1','x')
```

$$\text{ans} = -3 / (5 * \exp(2 * x)) - (2 * \cos(x)) / 5 - \sin(x) / 5$$

How to plot the solution of differential equation after you obtain the solution to the differential equation? Use **ezplot** See the following example.

Example 5: Solve

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} = \sin(x), y(0) = 1, y'(0) = 0$$

and plot the solution curve.

Solution:

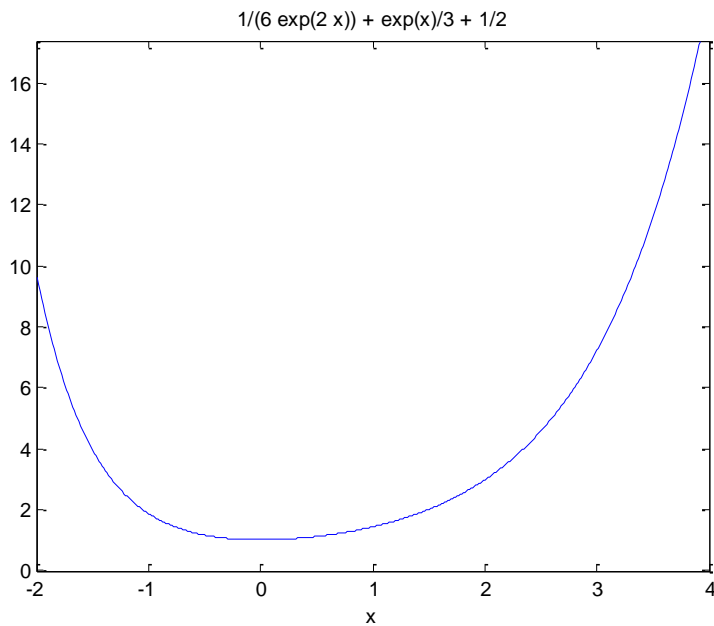
```
>> sol=dsolve('D2y+2*Dy=exp(x)', 'y(0)=1', 'Dy(0)=0', 'x')
```

sol =

$1/(6*\exp(2*x)) + \exp(x)/3 + 1/2$

```
>> ezplot(sol,[-2,4])
```

```
>>
```



Example 6: Solve

$$\frac{dy}{dt} = 2*y + t$$

and plot the solution curve with independent variable in [-2,0].

```
>> s=dsolve('Dy=2*y+t','y(0)=1','t')
```

s =

$$(5*\exp(2*t))/4 - t/2 - 1/4$$

```
>> ezplot(s,[-2,0])
```

